# POG Modeler: the Web Power-Oriented Graphs Modeling Program

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Abstract: In this paper the Power-Oriented Graphs (POG) technique is introduced and a new modeling program named "POG Modeler", freely available on the web, is presented. In the POG Modeler program the physical systems can be defined graphically using an ascii commend-line interface and referring to predefined graphic symbols. The POG Modeler automatically analyzes the given physical system and provides the following outputs: 1) the differential equations of the given system in symbolic form: 2) The POG block scheme of the considered system; 3) the Simulink block scheme of the given system ready for the Matlab environment. The POG systems are simple block schemes that can be easily used also by beginners.

Keywords: Dynamic modeling, Dynamic simulation, Linear systems, POG Modeling technique.

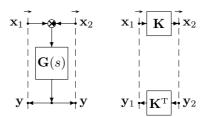
#### 1. INTRODUCTION

The Bond Graphs (BG) Paynter (1961), Karnopp et al. (2000), the Power-Oriented Graphs (POG) Zanasi (2010), Zanasi (1994) and the Energetic Macroscopic Representation (EMR) Bouscayrol ET AL. (2000), Mercieca ET AL. (2004) are graphical modeling techniques that use an energetic approach for modeling physical systems. The POG technique is based on the same energetic approach of the BG technique, but it uses a different graphical notation: instead of using the BG "bond/arrow" notation, it uses normal block diagrams for modeling the physical systems. The POG block schemes are easy to use, easy to understand and can be directly implemented in Simulink. The POG technique can be a useful tool for promoting the use of the energetic approach also between beginners and young researchers. A comparison between the BG, POG and EMR graphical techniques can be found in Zanasi et al. (2008). In this paper the basic concepts of POG modeling are introduced and the POG Modeler web side is presented. Examples of application of the POG graphical technique can be found in Zanasi (2010), Zanasi (1994), Morselli and Zanasi (2006), Zanasi et al. (2008), Zanasi and Grossi (2009) and Filippa et al. (2005) and the inside references.

# 2. THE POWER-ORIENTED GRAPHS TECHNIQUE

Basic blocks the POG technique uses only two basic blocks for modeling the physical systems, see Fig. 1: a) the elaboration block (e.b.) is used for modeling all the physical elements that store and/or dissipate energy (i.e. springs, masses, dampers, capacities, inductances,

resistances, etc.).
b) the **connection block** (c.b.) is used for modeling all the physical elements that "transform the power without losses" (i.e. neutral elements such as gear reductions,



a) Elaboration block b) Connection block

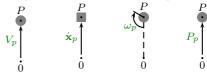
Fig. 1. POG blocks: elaboration block and connection block.

transformers, etc.). In the vectorial case matrix  ${\bf K}$  can also be rectangular, time varying or function of other variables.

**Power sections** the dashed lines in Fig. 1 represent the power sections which connect the two POG basic blocks with the external world. There are no restrictions on the choice of the vectors  $\mathbf{x}$  and  $\mathbf{y}$  involved in each dashed line except that the inner product  $\langle \mathbf{x}, \mathbf{y} \rangle = \mathbf{x}^{\mathrm{T}} \mathbf{y}$  must have the physical meaning of power flowing through the section.

Energetic domains the main energetic domains in modeling physical systems are: electrical, mechanical (translational and rotational) and hydraulic. Each energetic domain has its own couple of power variables, see Fig. 2.

**Power variables** they can be divided in two groups: 1) the "across-variables" (i.e. voltage  $V_p$ , velocity  $\dot{\mathbf{x}}_p$ , angular velocity  $\omega_p$  and pressure  $P_p$ ) which are defined "between two points P and 0" of the space:



2) The "through-variables" (i.e. current  $I_p$ , force  $F_p$ , torque  $\tau_p$  and volume flow rate  $Q_p$ ) which are defined "in each point P" of the space:

		Electrical	Mech. Tras.	Mech. Rot.	Hydraulic
	$\mathcal{D}_e$	C Capacitor	M Mass	J Inertia	$C_I$ Hyd. Capacitor
	$q_e$	Q Charge	p Momentum	p Ang. Momentum	V Volume
Across-Var.	$v_e$	V Voltage	v Velocity	$\omega$ Ang. Velocity	P Pressure
	$\mathcal{D}_f$	L Inductor	E Spring	E Spring	$L_I$ Hyd. Inductor
	$q_f$	$\phi$ Flux	x Displacement	$\theta$ Ang. Displacement	$\phi_I$ Hyd. Flux
Through-Var.	$v_f$	I Current	F Force	au Torque	Q Volume flow rate
	$\mathcal{R}$	R Resistor	b Friction	b Ang. Friction	$R_I$ Hyd. Resistor

Fig. 2. Energetic domains: the physical elements  $\mathcal{D}_e$ ,  $\mathcal{D}_f$  and  $\mathcal{R}$ ; the energy variables  $q_e$ ,  $q_f$ ; the power variables  $v_e$ ,  $v_f$ .

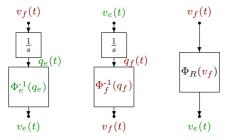


Fig. 3. Dynamic elements  $D_e$ ,  $D_f$  and static element R.



*Dynamic structure of the Energetic Domains* each energetic domains is characterized by only 3 different types of physical elements:

- 2 dynamic elements  $D_e$  and  $D_f$  which store the energy (capacitors, inductors, masses, springs, etc.);
- 1 static element R which dissipates (or generates) the energy (i.e. resistors, frictions, etc.);

The system dynamics can be described using 4 variables:

- 2 energy variables  $q_e$  and  $q_f$  which define how much energy is stored within the dynamic elements;
- 2 power variables  $v_e$  and  $v_f$  which describe the power flows entering or exiting the physical element.

The dynamic/static elements and the energy/power variables for the considered energetic domains are shown in Fig. 2. Note: the dynamic elements  $D_e$  provide the across power variables  $v_e$  as output, while the dynamic elements  $D_f$  provide the through power variables  $v_e$  as output.

Mathematical structure of the physical elements the dynamic element  $D_e$  is characterized by:

- 1) an internal energy variable  $q_e(t)$ ;
- 2) a through-variable  $v_f(t)$  as input variable;
- 3) an across-variable  $v_e(t)$  as output variable;
- 4) a constitutive relation  $q_e = \Phi_e(v_e)$  which links the internal variable  $q_e(t)$  to the output variable  $v_e(t)$ ;
- 5) a differential equation  $\dot{q}_e(t) = v_f(t)$  which links the internal variable  $q_e(t)$  to the input variable  $v_f(t)$ ;

The energy  $E_e$  stored in the dynamic element  $D_e$  is function only of the internal energy variable  $q_e$ :

$$E_e = \int_0^t v_e(t) \, v_f(t) \, dt = \int_0^{q_e} \Phi_1^{-1}(q_e) \, dq_e = E_e(q_e).$$

Integral Causality in the POG modeling technique all the dynamic elements are always described by block schemes using integral causality, see blocks in Fig. 3.

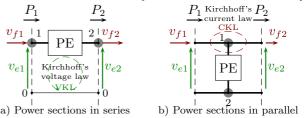


Fig. 4. Connections of the PE with the external world.

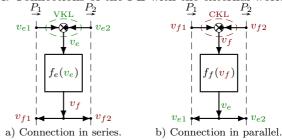


Fig. 5. POG schemes of the *series* and *parallel* connections.

Power sections in series and in parallel each Physical Element (PE) interacts with the external world through the power sections associated to its terminals. The two basic power connections of the physical element PE with the external world are shown in Fig. 4: a) the connection in series when the two terminals share the same through-variable  $v_f = v_{f1} = v_{f2}$ ; b) the connection in parallel when the two terminals share the same across-variable  $v_e = v_{e1} = v_{e2}$ .

The POG block schemes corresponding to the *series* and *parallel* connections reported in Fig. 4 are shown in Fig. 5:

- a) The summation element present in the POG block diagram of Fig. 5.a is a mathematical description of the Voltage Kirchhoff's Law (VKL) applied to the across variables  $v_{e1}$ ,  $v_{e2}$  and  $v_e$  involved in the closed path which is always present when the PE is connected in series, i.e. the green closed dashed path shown in Fig. 4.a.
- **b)** The summation element present in the POG block diagram of Fig. 5.b is a mathematical description of the Current Kirchhoff's Law (CKL) applied to the *through variables*  $v_{f1}$ ,  $v_{f2}$  and  $v_{f}$  involved in the "node" corresponding to terminal 1 of the PE connected in parallel, see the red closed dashed line shown in Fig. 4.b.

A simple example of POG modeling is shown in Fig. 6 where a C-parallel element is connected with an R-series element: this is a particular case of "Parallel - Series" connection: note the direct correspondence between the power sections ①, ② and ③ in the system and the dashed power sections ①, ② and ③ in the POG scheme.

**Example of POG modeling** a DC motor connected to an hydraulic pump is shown in Fig. 7. This system involves

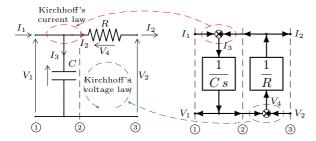


Fig. 6. POG modeling of an electrical RC circuit.

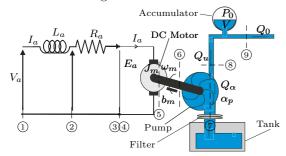


Fig. 7. A DC motor connected to an hydraulic pump.

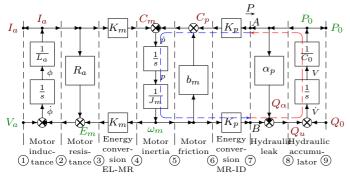


Fig. 8. POG scheme of the DC motor with hydraulic pump.

three different energetic domains: electrical, mechanical and hydraulic. The corresponding POG graphical representation in shown in Fig. 8: the power sections present in the POG scheme have a direct correspondence with the real physical sections. Let  $\mathbf{x} = [I_a \ \omega_m \ V_0]^{\mathrm{T}}$  be the state vector of the system, i.e. the output variables of the dynamic elements. From the POG scheme one directly obtains the following state space dynamic model  $\mathbf{L}\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{u}$ :

$$\underbrace{\begin{bmatrix} L_{a} & 0 & 0 \\ 0 & J_{m} & 0 \\ 0 & 0 & C_{0} \end{bmatrix}}_{\mathbf{I}} \underbrace{\begin{bmatrix} \dot{I}_{a} \\ \dot{\omega}_{m} \\ \dot{P}_{0} \end{bmatrix}}_{\dot{\mathbf{L}}} = \underbrace{\begin{bmatrix} -R_{a} - K_{m} & 0 \\ K_{m} & -b_{m} - K_{p} \\ 0 & K_{p} & -\alpha_{p} \end{bmatrix}}_{\mathbf{A}} \underbrace{\begin{bmatrix} I_{a} \\ \omega_{m} \\ P_{0} \end{bmatrix}}_{\mathbf{Y}} + \underbrace{\begin{bmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 1 \end{bmatrix}}_{\mathbf{U}} \underbrace{\begin{bmatrix} V_{a} \\ Q_{0} \end{bmatrix}}_{\mathbf{U}}$$
 (1)

where  $\mathbf{u}$  is the input vector and  $\mathbf{L}$ ,  $\mathbf{A}$  and  $\mathbf{B}$  are matrices that can be obtained by direct inspection of the POG scheme, see Zanasi (2010). In the considered case matrix  $\mathbf{L}$  is diagonal and its elements are the coefficients of the constitutive relations ( $\phi = L_a I_a$ ,  $p = J_m \omega_m$ ,  $V = C_0 P_0$ ) of the dynamic elements present in the system. The coefficients of matrices  $\mathbf{A}$  and  $\mathbf{B}$  are the gains of all the paths that link the state variables  $\mathbf{x}$  and the input variables  $\mathbf{u}$  to the inputs  $\dot{\phi}$ ,  $\dot{\omega}_m$ ,  $\dot{V}$  of the integrators present in the system.

**POG** block schemes satisfy the following properties 1) the energy  $E_s$  stored in the system can be expressed as  $E_s = \frac{1}{2} \mathbf{x}^T \mathbf{L} \mathbf{x}$ ; 2) the power  $P_d$  dissipated in the system can

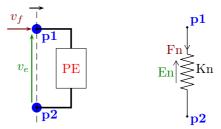


Fig. 9. The basic Physical Element "PE" of a POG system on the left, an electrical example on the right.

be expressed as  $P_d = \mathbf{x}^T \mathbf{A} \mathbf{x}$ ; 3) all the loops present in a POG block scheme contains an "odd" number of minus signs (i.e. of the black spots in the summation elements). 4) the direction of the power flowing through a section is positive if an "even" number of minus signs is present along one of the paths which goes from the input to the output of the section. Let us consider, for example, the power section ⑦ of Fig. 8: the power flows from left to right because the red dashed path that goes from B to A contains "zero" minus signs (i.e. an even number).

## 3. THE POG MODELER

The POG Modeler is a POG modeling program available on the web (http://zanasi2009.ing.unimo.it) which provides the POG symbolic dynamic model of a physical system when a graphical representation of the system is given.

3.1 POG Modeler: assumptions and physical elements.

Each Physical Element "PE" of a POG systems, see the left part of Fig. 9, is characterized by the following properties: 1) it interacts with the external world by means of two terminals  $\mathbf{p1}$  and  $\mathbf{p2}$ ; 2) the energy is stored or dissipated "within" the physical element; 3) the energy enters or exits the physical element only by means of the two power variables  $v_e$  and  $v_f$ .

The POG schemes are based on the following Assumptions: 1) The effort/across-variable  $v_e$  is positive if defined between terminals **p1** (top) and **p2** (bottom):  $v_e = v_{p1} - v_{p2}$ ; 2) The flow/through-variable  $v_f$  is positive if it enters terminal **p1** and exits terminal **p2**; 3) The power is positive if it enters the Physical element "PE".

The Physical Elements "PE" are identified by means of a two-digit string "xX":

- Electrical: (eC, eL, eR) and (eV, eI).
- Mechanical trans.: (mM, mK, mB) and (mV, mF).
- Mechanical rot.: (rJ, rK, rB) and (rW, rT).
- Hydraulic: (iC, iL, iR) and (iP, iQ).

The graphical representation of the "Internal Physical Elements" and the corresponding two-digits string "xX" are shown in Fig. 10. For each Energetic Domain there are only three "Internal Physical Elements": the two dynamic elements  $\mathcal{D}_e$  and  $\mathcal{D}_f$ , which store energy, and the static element  $\mathcal{R}$ , which dissipates energy.

The graphical representation of the "External Physical Elements" and the corresponding two-digits string "xX" are shown in Fig. 11. For each Energetic Domain there are only two "External Elements": 1) an across-generator

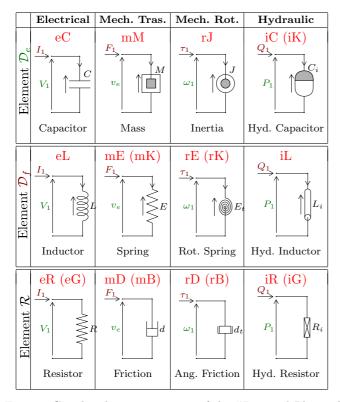


Fig. 10. Graphical representation of the "Internal Physical Elements" and the corresponding digit string "xX".

	Electric	Mech. Tras.	Mech. Rot.	Hydraulic
$\mathcal{G}_e$	${ m eV}$	$\mathrm{mV}$	${ m rW}$	iP
Across-generators	$V_1$ $V_1$ $V_1$ $V_1$ $V_1$ $V_2$ $V_3$ $V_4$	$\dot{x}_e \qquad \dot{x}_e$ Velocity Gen.	$\omega_1$ $\omega_1$ $\omega_1$ Ang. Velocity Gen.	$P_1 \longrightarrow P_1$ Pressure Gen.
$\mathcal{G}_f$	eI	${ m mF}$	m rT	iQ
Through-generators	$I_1$ $V_1$	$F_1$ $\dot{x}_e$	$\tau_1$ $\omega$ $\omega_1$	$Q_1$ $P_1$
$\overline{\mathrm{Thro}}$	Current Gen.	Force Gen.	Torque Gen.	Flow Rate Gen.

Fig. 11. Graphical representation of the "External Physical Elements" and the corresponding digit string "xX".

 $\mathcal{G}_e$  which generates the power across-variable  $v_e$ ; 2) a through-generator  $\mathcal{G}_f$  which generates the power through-variable  $v_f$ . The "External Elements" describe how the external world acts on the considered system.

#### 3.2 POG Modeler: the Web Site.

The **POG Modeler** is available on the web at the following address: <a href="http://zanasi2009.ing.unimo.it">http://zanasi2009.ing.unimo.it</a>. The use of the program is free, but the registration is required.

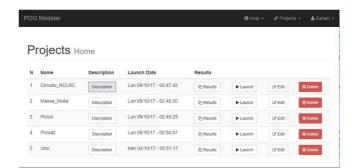


Fig. 12. Example of layout of the user home page.

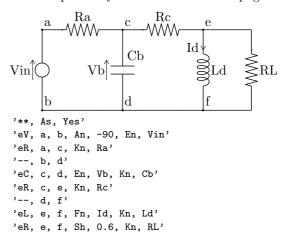


Fig. 13. Electrical example: the physical system and the corresponding "command-lines".

An example of layout of the user home page is shown in Fig. 12.

A Physical System can be introduced in the POG Modeler using an ascii "command-lines" interface. The electric circuit shown in the upper part of Fig. 13, for example, can be defined in the POG Modeler interface by using the ascii "command-lines" shown in the lower part of Fig. 13.

There are two types of command-lines:

1) the "system command-lines", such as '\*\*, As, Yes', which define commands and parameters that apply to all the physical elements of the considered system. The "system command-lines" have the following structure:

$$\underbrace{\text{Mandatory}}_{**, \mathbf{Par1}, \mathbf{Val1}} \underbrace{\text{Optional}}_{[, \mathbf{Par2}, \mathbf{Val2}]} \underbrace{[, \mathbf{Par3}, \mathbf{Val3}]}_{[, \mathbf{Par3}, \mathbf{Val3}]} \cdots$$

The initial string "\*\*" identifies the line as a "system command-line". Each couple ", Parx, Valx" is composed by a system parameter "Parx" and its value "Valx". At least one couple ", Par1, Val1" has to be present in each "system command-line". The command-line '\*\*, As, Yes', for example, tells to the POG Modeler "compute the symbolic differential equations of the considered system".

2) the "element command-lines", such as 'eR, a, c, Kn, Ra', which introduce new Physical Elements in the POG physical scheme and define their parameters. The "element command-lines" have the following structure:

Mandatory Optional 
$$(XX, p1, p2)$$
  $(Par1, Val1)$   $(Par2, Val2)$   $\cdots$ 

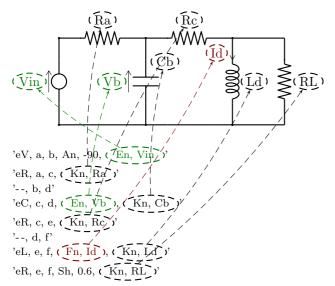


Fig. 14. How to set the names of the system parameters.

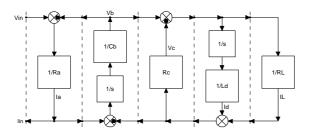


Fig. 15. "POG, Si" provides the POG block scheme.

The two-digits string "xX" uniquely identifies the Physical Element. The two ascii labels p1 and p2 identify the positions of the first and second terminal of the the Physical Element. The command lines '--, b, d' and '--, d, f' present in the lower part of Fig. 13 are meant to tell the POG Modeler to introduce straight lines between the two nodes (b, d) and the two nodes (d, f), respectively.

Each optional term "[, Parx, Valx ]" is composed by the name "Parx" of a parameter of the Physical Element, and its value "Valx". The list and the meaning of all the "system" and "element " commands of the POG Modeler can be found in the *Help Menu* of the user *Home Page*, together with a *Manual* which describes the basic properties of the program.

Each Physical Element is characterized by an across-variable  $v_e$ , a through-variable  $v_f$  and an internal-parameter  $\mathcal{K}$ , see the right part of Fig. 9. The names of the across-variable  $v_e$ , the through-variable  $v_f$  and the internal-parameter  $\mathcal{K}$  can be defined by using the parameters "En", "Fn" and "Kn", respectively, see Fig. 14.

The POG Modeler provides the following important commands: 1) "POG, Si" provides the POG block scheme of the considered Physical System, see Fig. 15. 2) "SLX, Si" provides the Simulink block scheme of the considered Physical System, see Fig. 16. 3) "As, Si" provides the symbolic differential equations of the considered system:

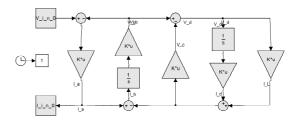


Fig. 16. "SLX, Si" provides the Simulink block scheme.

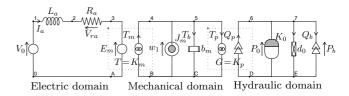


Fig. 17. POG representation of the system shown in Fig. 7.

```
R_L/(R_L+R_c), -(R_L*R_c)/(R_L+R_c)];
B=[ 1/R_a; 0 ];
C=[ -1/R_a, 0 ];
D=[ 1/R_a ]
X=[ V_b; I_d ];
U=[ V_i_n ];
Y=[ I_i_n ]
```

#### 3.3 POG Modeler: a multidomain example.

Let us now refer to the physical system shown in Fig. 7 which involves three different energetic domains: electrical, mechanical and hydraulic. The POG symbolic representation of this system in shown in Fig. 17. This symbolic representation has been obtained using the following command-lines:

```
'**, Sn, Si, Lw, 0.7'
'eV, 1, 0, An, -90, En, V_0, Fn, L_0'
'eL, 1, 2, Ln, 0.7, Zm,0.9, Kn, L.a, Fn, L.a'
'eR, 2, 3, Ln, 0.7, Zm,0.9, En, V_r_a, Kn, R_a'
'--, 0, A, Ln, 1.4'
'CB, [3; 4], [A; B], Kn, F2=K_m*F1, En, [E_m;w_2], Fn, [I_1;T_m], Sh, [0.2;-0.2], La,0.3'
'rJ, 4, B, Sh, 0.4, Kn, J_m, En, w_1'
'--, 4, 5, Ln, 0.8'
'--, B, C, Ln, 0.8'
'rB, 5, C, Kn, b_m, Fn, T_b'
'CB, [5; 6], [C; D], Kn, F1=K_p*E2, En, [w_1;p_2], Fn, [T_p;Q_p], Sh, [0.5;-0.2], La,0.3'
'iK, 6, D, Kn, K_0, En, P_0, Sh, 0.4'
'--, 6, 7, Ln, 0.8'
'--, D, E, Ln, 0.8'
'--, D, E, Kn, d_0, Fn, Q_d'
'iQ, 7, E, Kn, d_0, Fn, Q_d'
'iQ, 7, E, En,-P_b, Fn, Q_b, Sh, 0.4, Pin, 1, ShY,Si, FnY,9'
```

The electrical part of the system is characterized by the physical elements 'eV', 'eL' and 'eR'. The mechanical rotational part of the system is composed by the elements 'rJ' and 'rB'. The hydraulic part of the system is composed by 'iK', 'iG', and 'iQ'.

The physical elements identified by the two-digits string "CB" are the "Connection Blocks". These blocks connect two different Energetic Domains without storing or dissipating energy. The first connection block 'CB, [3; 4], [A; B]' converts electric power to mechanical rotational power, and viceversa. The second connection block 'CB, [5; 6], [C; D]' converts mechanical rotational power to hydraulic power.

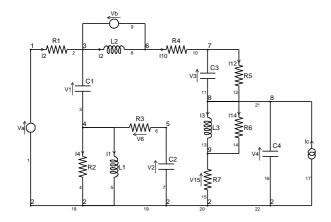


Fig. 18. Example of a large electric circuit.

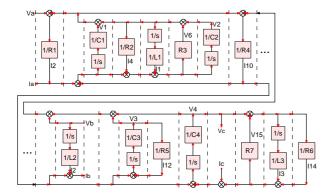


Fig. 19. POG scheme of the electric circuit of Fig. 18.

The string "Kn, F2=K\_m\*F1" present within the first connection block means that the Flow/Through variable F2 of the output power section is obtained multiplying the Flow/Through variable F1 of the input power section by the internal parameter "K\_m":

$$F2=K_m*F1 \Rightarrow T_m = K_m I_1, E_m = K_m w_2.$$

The string "Kn, F1=K\_p\*E2" present within the second connection block means that the Flow/Through variable F1 of the input power section is obtained multiplying the Effort/Across variable E2 of the output power section by the internal parameter "K\_p":

$$\mathbf{F1} = \mathbf{K}_{-p} * \mathbf{E2} \qquad \Rightarrow \qquad T_p = K_p P_0, \quad Q_p = K_p w_1.$$

The POG Modeler can both analyze simple and complex systems. The large electric circuit shown in Fig. 18, for example, can be easily analyzed by the POG Modeler: the corresponding POG block scheme is shown in Fig. 19.

Finally, let us consider the hydraulic circuit shown in Fig. 20. The corresponding POG block scheme provided by the POG Modeler is shown in Fig. 19.

# 4. CONCLUSIONS

In this paper the POG technique has been introduced and the modeling program named "POG Modeler", freely available on the web, has been presented. Using the POG Modeler one can obtain automatically the following outputs: 1) the differential equations in form of the given system: 2) The POG block scheme of the given system; 3) the Simulink block scheme of the given system suitable

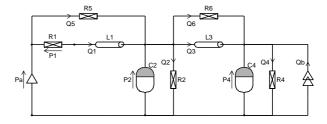


Fig. 20. Example of an hydraulic circuit.

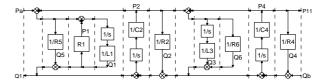


Fig. 21. POG scheme of the hydraulic circuit of Fig. 20.

to be run in Matlab. The POG block schemes are easy to use, easy to understand and can be directly implemented in Simulink. The POG technique can be easily used also by beginners.

The Reviewers, if they wish, can log in anonymously the POG Modeler (http://zanasi2009.ing.unimo.it) using US: Anonymous and PW: pogmodeler. In the Home page they will find the examples presented here.

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